

## 扇形面積與弧長

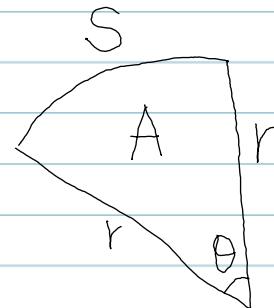
(1) 設一扇形的半徑為8公分，所對的圓心角為 $60^\circ$ ，求(a) 扇形弧長 (b) 扇形面積

Sol. (a)  $S = r \cdot \theta$

$$= 8 \cdot \frac{\pi}{3} = \frac{8}{3}\pi$$

(b)  $A = \frac{1}{2} r^2 \cdot \theta$

$$= \frac{1}{2} \cdot 64 \cdot \frac{\pi}{3} = \frac{32\pi}{3}$$



$$\begin{aligned} S &= r \cdot \theta \quad (\text{弧度}) \\ A &= \frac{1}{2} r^2 \theta \end{aligned}$$

(2) 設一扇形弧長為 $8\pi$ ，面積為 $40\pi$ ，則此扇形的(a) 周長 (b) 圓心角各為多少？

Sol.  $S = 8\pi, A = 40\pi$

$$S = r \cdot \theta$$

$$\frac{40\pi}{5} = \frac{1}{2} r \cdot 8\pi$$

$$\begin{aligned} A &= \frac{1}{2} r^2 \cdot \theta \\ &= \frac{1}{2} r \cdot S \end{aligned}$$

$$r = 10$$

(a)  $S = 8\pi, r = 10$

$$20 + 8\pi$$

(b)  $8\pi = 10 \cdot \theta \Rightarrow \theta = \frac{8\pi}{10} = \frac{4\pi}{5}$

